

by Ahrens (1952), but is in fairly good agreement with the values in Table 5 derived from the ionic distances W-O known in the $[\text{WO}_4]^{2-}$ ion of the structures AWO_4 ($A = \text{Ba}, \text{Ca}, \text{Pb}$ or Sr) given by Sillén & Nylander (1943).

Table 5 shows also the change of the ionic distances in the tetrahedral coordination with the radii, or with the polarization effect of the A cations. Also the NH_4^+ ion must have such an effect complicated to some extent by the protons around the N atom. The reduced ionic distance of W-O, as well as that of W-S can be attributed most probably to a partially covalent bond in the tetrahedron.

According to Fig. 4 and Table 4 the NH_4^+ ions have 9 and 10 nearest neighbours respectively, with distances ranging from 3.10 to 3.96 Å. The arrangement of the S^{2-} ions around NH_4^+ is rather irregular.

Although the structure of ammonium thioungstate cannot be regarded as a close-packed one, a similarity to close packing can be detected. Parallel to the plane (100) corrugated ionic planes can be seen (broken lines show these planes for one period in Fig. 4), built up of S^{2-} and NH_4^+ ions and appearing with two different ionic arrangements given without distortion in Fig. 5. These two kinds of ionic plane A and B alternate in the crystal lattice according to the scheme $\dots \text{ABBABBA} \dots$. In Fig. 4 the period BABB is given. The fitting of any two neighbouring ionic planes is pictured in Fig. 6(a), (b), (c) in which the distortion of the lattice is omitted. As the ionic planes are built up of S^{2-} anions and NH_4^+ cations in one (a, b) period of the unit cell, by fitting the AB and BA planes, only one tetrahedron and by fitting the BB planes, two tetrahedra are built with only S^{2-} ions at the

corners. Every other polyhedron of this ionic arrangement has at its corners different kinds of ions. If we put W atoms in the cavities surrounded only by S^{2-} ions and make a distortion by corrugating the related ionic planes which is necessary in order to separate from each other the atoms that are too near to one another in the undistorted arrangement, we come to the structure of ammonium thioungstate.

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Order in Binary σ -Phases

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The atomic order in two σ -phase Re-Mo alloys has been determined using powder photographs and X-ray diffractometry. The proposed order schemes support the same correlation between the position of the element in the periodic table and the lattice site as that obeyed by σ -phases formed by elements of the first long period. Rhenium is similar to manganese in its ordering behaviour.

Introduction

The existence of the σ -phase in many binary and ternary alloys of the transition elements has been reported in recent years (Greenfield & Beck, 1956; Knapton, 1957; Nevitt & Downey, 1957) and the detailed structure of this phase has been carefully

determined for several representative alloys (Bergman & Shoemaker, 1954; Kasper, Decker & Belanger, 1952; Dickins, Douglas & Taylor, 1956). The existence of order in the σ -phase structure has been established in a number of alloys (Decker, Waterstrat & Kasper, 1954; Kasper & Waterstrat, 1956; Ageev & Shekhtman, 1959, 1960; Brown & Forsyth, 1961; Wilson &

Spooner, 1963). The aim of these investigations is to obtain information about the factors governing the structure of this phase.

The present X-ray investigation was carried out in order to determine the nature of the order present in the σ -phase formed by rhenium and molybdenum

since there is a large difference in the atomic numbers of these two elements ($Z_{\text{Re}} - Z_{\text{Mo}} = 33$). The σ -phases were prepared by arc-melting in argon. The nominal compositions of the two alloys used were Re 55 at.%, Mo 45 at.% (ReMo55) and Re 68 at.%, Mo 32 at.% (ReMo68). According to Greenfield & Beck (1956)

Table 1. X-ray data for σ -WRe 50

<i>hkl</i>	Powder camera $\sin^2 \theta \times 10^4$		Intensities		Diffractometer intensities		
	Obs.	Calc.	Obs.	Calc.	Obs.	Calc.	
110	—	128	—	<0.1	—	0.1	
200	—	256	—	<0.1	—	0.1	
101	—	300	—	4.8	—	4.7	
210	—	321	—	<0.1	—	0.1	
111	—	365	—	0.9	—	0.8	
220	—	513	—	<0.1	—	0.1	
211	—	557	—	0	—	0	
310	—	641	—	1.1	—	0.6	
221	—	749	—	3.9	—	1.7	
301	—	813	—	1.3	—	0.5	
320	—	834	—	0.7	—	0.3	
311	884	887	<i>vw</i>	41.8	18	16.2	
002	951	945	<i>w</i>	167	47	55.7	
400	—	1026	—	0.2	—	0.1	
321	—	1070	<i>vwv*</i>	4.6	233	1.5	231
112	—	1073		21.5		6.6	
410	1098	1090	<i>s</i>	734	223	223	
330	1160	1154	<i>m</i>	358	101	103	
202	1207	1202	<i>m</i>	319	92	90	
212	1273	1266	<i>s</i>	679	183	180	181
420		1282	—	2.2		0.6	
411	1334	1326	<i>vs</i>	1070	268	274	
331	1398	1390	<i>s</i>	534	129	129	
222	1464	1458	<i>w</i>	138	31	31.8	
421	—	1519	—	5.8	—	1.3	
312	1586	1586	<i>w</i>	174	36	36.7	
430	—	1603	—	0.8	—	0.2	
510	—	1667	—	4.7	—	1.0	
322	1786	1779	<i>vw</i>	43.9	9	8.5	
501	1842	1839	<i>vw</i>	3.2	10.4	0.6	9.4
431				46.9		8.8	
520	—	1859	—	<0.1	—	<0.1	
511	1909	1903	<i>vw</i>	46.7	8.1	8.5	
402	—	1971	—	6.4	—	1.1	
412	—	2035	—	4.8	—	0.8	
440	—	2052	—	0.1	—	0.2	
521	2098	2096	<i>vwv</i>	19.3	7	3.2	3.3
332		2099		0.83		0.1	
530	—	2186	—	2.6	—	0.4	
103	—	2191	—	2.0	—	0.3	
422	—	2228	—	1.06	—	0.2	
113	—	2255	—	0.3	—	<0.1	
441	—	2288	—	0.2	—	<0.1	
600	—	2308	—	0.4	—	<0.1	
610	—	2372	—	<0.1	—	<0.1	
531	—	2416	—	<0.1	—	<0.1	
213	—	2447	—	<0.1	—	<0.1	
432	2553	2548	<i>vw</i>	59.8	11	8.74	9.6
620		2565		5.8		0.83	
611	2617	2609	<i>vw</i>	1.2	10	0.17	9.3
512		2612		65.3		9.17	
540	—	2629	—	4.9	—	0.7	
223	—	2640	—	1.9	—	0.2	
303	—	2704	—	0.6	—	0.1	
313	—	2768	<i>vwv*</i>	21.4	—	2.8	
621	2808	2801	<i>w</i>	29.6	19	3.75	21.4
522		2805		139.6		17.64	

* Not measurable but visible.

v = very; *w* = weak; *m* = medium; *s* = strong.

these σ -phases are stable above 1,200 °C and, accordingly, the melts were annealed at 2,000 °C before quenching. The alloys were extremely brittle and powder samples were prepared by crushing and grinding with an agate mortar.

In addition to the two rhenium-molybdenum alloys a sample of a σ -phase containing 50 at.% tungsten and 50 at.% rhenium (WRe50) was also submitted to X-ray examination. Since the difference in scattering factors of tungsten and rhenium is very small and the anomalous dispersion corrections for copper radiation are the same (Dauben & Templeton, 1955), this sample behaved as though it were disordered and thus served as a kind of standard for the detection of order in the rhenium-molybdenum alloys.

Experimental

Debye-Scherrer powder photographs of all the alloys were taken with a 19 cm precision camera using a copper target with nickel filter. Unit-cell sizes were obtained from the observations on high-angle lines using a Nelson-Riley extrapolation method. Line intensities were estimated visually up to $\sin^2 \theta = 0.4$. Beyond this limit the interference between α_1 and α_2 components of neighbouring lines made the estimation of line intensities difficult. Line intensities were calculated for various ordering schemes and for a random atom distribution in the unit cell using the atomic co-ordinates of σ Fe-Cr given by Bergman & Shoemaker (1954). Other investigations (Decker *et al.*, 1954; Kasper & Waterstrat, 1956) have shown that these co-ordinates can be used with reasonable confidence with other σ -phases and their use should not introduce any serious error in intensity calculations for low hkl . The anomalous-dispersion corrections to scattering factors given by Dauben & Templeton (1955) have been included in all the calculations. An absorption correction for each alloy has been determined using the method described by Klug & Alexander (1954).

In order to obtain quantitative estimates of line intensities several runs were made with flat powder samples using a Hilger diffractometer with a stabilized Philips X-ray set and a curved quartz-crystal monochromator. Copper radiation was used with a xenon-filled proportional counter as detector connected to a single-channel pulse analyser set to received pulses from $K\alpha$ photons only. The diffraction pattern was recorded continuously at a chart speed of 3.75° of 2θ per hour.

The line intensities of the diffractometer specimens were determined by measuring the areas beneath peaks using a planimeter. These were compared with calculations based on the Bergman-Shoemaker parameters. The absorption factor was assumed constant over the range of 2θ measured (10° to 80° approx.). Preferred-orientation effects, which were troublesome with the WRe sample, were minimized by mixing the

finely powdered sample with starch. The slight disagreement between observed and calculated intensities for 002 and 004 lines (Table 1) is attributed to this effect. The same procedure was adopted for the ReMo samples.

The diffractometer was set with an exit slit giving a horizontal divergence of 0.34°. With a time constant of five seconds and a thin sample of quartz powder which was used for calibration, the resolving power of the 20 $\bar{2}$ 0 line at 42° (approx.) was 3%. The use of Soller slits to improve the resolution was precluded because of the very small quantities of σ -phase samples available. Although reproducible results were obtained with the sample-starch mixtures, the intensities of medium and strong lines could not be estimated with an accuracy better than 10%; the weakest lines, which were most important in σ -phase order determination, could not be measured to better than 30 to 40%. The σ -phase is complex and the small intensity contributions from extremely weak lines, such as the unobserved lines of Table 1, give rise to a virtual background which makes the delineation of the 'wings' of measured lines somewhat uncertain. This effect, coupled with the asymmetry of line profiles, led to large uncertainties in very weak line intensities. The uncertainties in single runs were reduced by taking mean values from several runs.

Results

(i) σ -Phase WRe50

The unit-cell dimensions are

$$a = 9.6274 \pm 0.0005, \quad c = 5.0150 \pm 0.0005 \text{ \AA}, \\ c/a = 0.5209.$$

This result is in good agreement with Greenfield & Beck (1956) who give $a = 9.55$, $c = 4.98$ Å, $c/a = 0.52$, for the WRe σ -phase. The values of $\sin^2 \theta$ and line intensities are given in Table 1. The good agreement between observed and calculated intensities, assuming a random distribution of atoms in the unit cell, gives some justification for using the Bergman & Shoemaker parameters.

(ii) σ -Phase ReMo55

The unit-cell dimensions are

$$a = 9.6010 \pm 0.0005, \quad c = 4.9850 \pm 0.0005 \text{ \AA}, \\ c/a = 0.5192.$$

Previous investigators of this σ -phase quote: $a = 9.54-9.58$, $c = 4.95-4.96$ Å, $c/a = 0.52$ (Greenfield & Beck, 1956); $a = 9.54$, $c = 4.95$ Å, $c/a = 0.52$ for Re_3Mo_2 (Ageev & Shekhtman, 1959); $a = 9.588$, $c = 4.983$ Å, $c/a = 0.520$ for Re_3Mo_2 (Knapton, 1958).

Visual comparison of the WRe50 and ReMo55 Debye-Scherrer films shows only minor differences in the intensities of the two characteristic groups of strong σ -phase lines and on this evidence alone the

ReMo55 phase might be regarded as completely disordered. A comparison of overexposed films shows the following differences which are attributed to ordering:

From the composition of the alloy it is assumed than an average of 16.5 atoms of rhenium and 13.5

atoms of molybdenum are contained in the unit cell. The order scheme was determined by trial and error, guided by the requirements listed in Table 2. The relatively weak 002 line suggested that some Re atoms occupied *E* sites which have a negative structure amplitude. In order that 331 might be strong the *D* sites must be mainly occupied by Re atoms. Likewise, the observed intensity of 101 required

Table 2. Comparison of selected weak lines on ReMo55 and WRe50 films

<i>hkl</i>	$\sin^2 \theta$	Remarks
101	309	Much stronger on ReMo55 than WRe50
111	374	Seen on ReMo55 but not on WRe50
311	887	Much weaker on ReMo55 than WRe50
322	1786	This group of lines is relatively much stronger on ReMo55 than WRe50
131	1843	
511	1908	
402	1999	Easily seen on ReMo55 film but not on WRe50 film
432	2576	This pair of lines is appreciably weaker on ReMo55 than WRe50
611	2638	
512	2638	

Table 3. Order scheme for ReMo55

Crystallographic site	Total no. of atoms	Site occupancy Re	Mo
<i>A</i> (000)	2	2	Nil
<i>B</i> (<i>xx</i> 0) (<i>x</i> =0.3981)	4	1	3
<i>C</i> (<i>xy</i> 0) (<i>x</i> =0.4632) (<i>y</i> =0.1316)	8	4	4
<i>D</i> (<i>xy</i> 0) (<i>x</i> =0.7376) (<i>y</i> =0.0653)	8	6.5	1.5
<i>E</i> (<i>xxz</i>) (<i>x</i> =0.1823) (<i>z</i> =0.25)	8	3	5

Table 4. X-ray data for σ -ReMo 55

<i>hkl</i>	Powder camera $\sin^2 \theta \times 10^4$		Intensities: calculated			Diffractometer Intensities: calculated		
	Obs.	Calc.	Observed	Ordered	Random	Observed	Ordered	Random
	110	—	129	—	—	—	—	< 0.1
200	—	258	—	0.3	—	—	0.3	< 0.1
101	309	304	<i>vvw</i>	20.3	3.2	18	19.2	3.0
210	—	322	—	0.6	—	—	0.5	< 0.1
111	374*	368	<i>vvvw</i>	4.1	0.6	4.6	3.4	0.5
220	—	516	—	0.9	—	—	0.5	< 0.1
211	—	561	—	—	—	—	< 0.1	0
310	—	645	—	0.6	0.8	—	0.3	0.4
221	—	755	—	1.3	2.8	—	0.5	1.1
301	—	819	—	—	0.9	—	< 0.1	0.3
320	—	838	—	1.3	0.5	—	0.5	0.2
311	887	884	<i>vvvw</i>	16.1	30.1	5.8	5.4	10.1
002	952	957	<i>mw</i>	140	113	38	44.3	35.5
400	—	1032	—	1.3	0.4	—	0.4	0.1
321	—	1077	—	1.0	3.3	—	0.3	0.9
112	1093	1086	<i>vs</i>	13	533	15.2	3.6	4.2
410		1096		520				
330	1157	1160	<i>ms</i>	257	256	70	65.6	65.2
202	1211	1214	<i>m</i>	218	227	57	55.1	57.4
212	1276	1279	<i>s</i>	482	490	475	116	115
420		1289		7.6				
411	1332	1335	<i>vvs</i>	837	755	194	193	174
331	1397	1400	<i>s</i>	415	376	98	92.3	83.7
222	1467	1472	<i>m-mw</i>	97	91	23	20.8	19.6
421	1528*	1528	<i>vvvw</i>	3.1	4.0	—	0.6	0.8
312	1596	1601	<i>m</i>	134	136	115	27.3	23.5
430		1602		2.3				
510	1680*	1676	—	6.3	3.2	—	1.2	0.6
322	1786	1795	<i>w</i>	49.1	28.8	10.4	9.2	5.4
501	1843	1851	<i>w</i>	4.5	55.2	2.1	0.8	0.4
431				50.7				
520	—	1870	—	—	—	—	< 0.1	< 0.1
511	1908	1915	<i>w</i>	49.2	31.5	9.4	8.8	5.7
402	1999*	1988	<i>vvvw</i>	14.8	4.2	3.9	2.6	7.4
412	2062*	2052	<i>vvvw</i>	12.7	12.9	3.2	2.1	0.5
440		2063		0.2				
521	2101	2109	<i>vvw</i>	19.5	23.5	12.7	3.1	2.0
332		2117		4.0				
530	—	2192	—	0.3	1.7	—	< 0.1	0.3
103	2222	2217	<i>vvvw</i>	8.3	1.3	—	1.3	0.2
422	—	2246	—	1.2	0.7	—	0.2	0.1

Table 4 (cont.)

<i>hkl</i>	Powder camera $\sin^2 \theta \times 10^4$		Intensities: calculated			Diffractometer Intensities: calculated			
	Obs.	Calc.	Observed	Ordered	Random	Observed	Ordered	Random	
113	—	2281	—	1.8	0.3	—	0.3	<0.1	
441	—	2302	—	1.0	0.1	—	0.2	<0.1	
600	—	2321	—	—	0.3	—	0	<0.1	
610	—	2385	—	0.7	—	—	0.1	<0.1	
531	—	2431	—	—	—	—	<0.1	<0.1	
213	—	2494	—	—	—	—	<0.1	<0.1	
432	2576*	2568	<i>vvvw</i>	23.6	24.2	39.6	5.4	5.5	6.0
620		2579		0.6				3.9	
611	2638*	2624	<i>vvvw</i>	1.1	26.4	2.3	5.2	0.3	6.1
512		2633		25.3				43.2	
540	—	2643	—	0.3	—	3.1	—	0.4	
223	—	2668	—	0.6	—	2.6	—	0.2	
303	—	2732	—	—	—	0.4	—	<0.1	
313	2818	2797	<i>vw</i>	7.2	93.3	13.9	8.0	0.9	1.8
621		2818		12.0		19.7		2.5	
522		2826		74.1		72.4		9.1	
541	2889*	2878	<i>vvvw</i>	6.6	7.3	6.6	—	1.7	1.7
630		2896		0.7				13.8	
323	—	2985	—	—	—	—	—	0.1	
442	—	3015	—	—	—	—	—	0.1	
.....									
631	3140	3135	<i>m-ms</i>	7.9	291	11.1	30.1	0.9	1.3
532		3143		283		298		33.8	
550	3214	3218	<i>w-mw</i>	112	114	116	—	0.3	0.1
710		—		—		2.4		0.2	
413	3242	3243	<i>ms-s</i>	417	—	377	124	47	42.4
602	3268	3272	<i>m</i>	154	—	162		17	17.9
333	3303	3307	<i>m</i>	218	—	198	115	23.7	21.5
612	3332	3336	<i>m</i>	137	137	134		14.5	14.2
640		3347		0.4		0.8	<0.1	<0.1	
701	3407	3393	<i>ms</i>	25	303	24	—	2.5	2.4
720		3411		278		296		30.3	
423	—	3436	—	5.5	—	3.6	45.5	28.4	30.3
711	3453	3457	<i>m</i>	1.1	190	0.3		0.6	0.4
551		—		—		189	162	<0.1	<0.1
622	3527	3529	<i>w</i>	108	—	95	11.8	19.2	16.4
641	3590	3586	<i>w</i>	28	129	23		10.7	9.5
542		3594		101		88	2.8	2.3	
721	3646	3650	<i>ms</i>	292	—	230	12.5	9.9	8.7
730	—	3733	—	0.8	—	0.2		26.3	28.6
503	3777*	3764	<i>vvvw</i>	2	27.6	0.7	—	0.1	0.1
433		—		—		25.6		19.3	0.2
004	3819	3820	<i>m</i>	222	256	213	16.9	2.4	1.8
513		3822		33.5		22		20.1	19.2

N.B. Values of $\sin^2 \theta$ below dotted line refer to α_1 components. *v* = very; *w* = weak; *m* = medium; *s* = strong.
* Indicates measurement made on overexposed film.

B sites to be filled mainly by molybdenum atoms and *A* sites filled by Re atoms. The refinement of an order scheme which satisfied the powder film data was obtained from a study of diffractometer intensities. The reliability of the final order scheme, which is given in Table 3, is such that a replacement of one atom of Re by Mo has an observable adverse effect. The calculated intensities for this scheme, normalized to the diffractometer intensities, and also for a random arrangement are given in Table 4; the powder film data are also given in this table.

(iii) σ -Phase ReMo68

The unit-cell dimensions are

$$a = 9.5788 \pm 0.0004, \quad c = 4.9741 \pm 0.0005 \text{ \AA}, \\ c/a = 0.5193.$$

This cell is slightly smaller than that of ReMo55, which supports the belief that Re atoms tend to occupy sites of smaller volume than those of Mo atoms.

Table 5. Order schemes for ReMo68

Site	Total no. atoms	Order scheme No. 1		Order scheme No. 2	
		Re	Mo	Re	Mo
<i>A</i>	2	2	Nil	2	Nil
<i>B</i>	4	2	2	1	3
<i>C</i>	8	4	4	4	4
<i>D</i>	8	8	Nil	8	Nil
<i>E</i>	8	4	4	5	3

Table 6. X-ray data for σ -ReMo 68

<i>hkl</i>	Powder camera $\sin^2 \theta \times 10^4$		Intensities: calculated				Diffractometer Intensities: calculated			
	Obs.	Calc.	Obs.	Ord. 1	Ord. 2	Random	Obs.	Ord. 1	Ord. 2	Random
101	307	308	<i>vvw</i>	19.1	26.3	3.4	18.6	18.1	24.9	3.2
111	—	373	< <i>vvw</i>	5.5	7.1	0.6	4.3	4.6	5.9	0.5
311	896	895	< <i>vvw</i>	17.5	12.9	32.3	6.8	5.9	4.3	10.8
002	965	968	<i>w</i>	158	139	121	41.9	50	43.8	38.1
112 } 410 }	1107 } 1109 }	1096 } 1109 }	<i>s</i>	11.2 } 597.6 }	16 } 620 }	609 } 636 }	572 } 169 }	3.4 } 165 }	169 } 176 }	157 } 157 }
330	1172	1174	<i>m</i>	278	293	274	81	70.9	75	70
202	1225	1226	<i>mw</i>	249	244	243	59.9	62.7	62	61.5
212 } 420 }	1289 } 1304 }	1291 } 1304 }	<i>ms</i>	536 } 10 }	542 } 11 }	553 } 513 }	128 } 128 }	129.2 } 2.2 }	131 } 134 }	124 } 124 }
411	1348	1349	<i>vs</i>	922	881	809	209	213	203	187
331	1413	1414	<i>ms</i>	484	458	403	103	108	102	90
222	1483	1485	<i>vw</i>	117	126	98	26.5	25	26.9	21
421	1543	1544	< <i>vvw</i>	3.9	7.1	4.3	not obs.	0.8	1.5	0.9
312 } 430 }	1614 } 1629 }	1614 } 1629 }	<i>w</i>	146 } 3 }	150 } 5 }	155 } 124 }	29.4 } 29.4 }	29.7 } 0.6 }	30.3 } 31.6 }	25.3 } 25.3 }
322	1807	1809	<i>vw</i>	48.5	64.3	30.9	10.7	9.1	12.1	5.8
501 } 431 }	1865 } 1869 }	1869 } 1869 }	<i>vw</i>	4.1 } 44.3 }	6.6 } 53.6 }	60.2 } 35.7 }	10.2 } 10.2 }	0.7 } 8.1 }	8.8 } 11 }	6.5 } 6.5 }
511	1930	1934	<i>vw</i>	61	61	33.8	11.4	10.9	10.9	6.1
402	—	2004	<i>vvw</i>	14.7	19.9	4.5	2.8	2.6	3.5	7.9
412	—	2069	< <i>vvw</i>	13.1	6.2	3.4	2.5	2.1	1.0	0.5
521 } 332 }	2122 } 2134 }	2128 } 2134 }	<i>vvw</i>	24 } 2.4 }	20.8 } 1.5 }	22.3 } 14.2 }	5.0 } 5.0 }	3.9 } 0.4 }	4.3 } 3.5 }	2.3 } 2.3 }
103	2235	2230	<i>vvw</i>	8.6	10.5	1.4	not obs.	1.4	1.7	0.2
432 } 630 }	2586 } 2602 }	2588 } 2602 }	<i>vvw</i>	25.3 } 1.4 }	23.4 } 1.9 }	25.3 } 46.6 }	4.5 } 4.5 }	3.2 } 0.3 }	3.5 } 3.6 }	6.4 } 6.4 }
611 } 512 }	2647 } 2653 }	2647 } 2653 }	<i>vvw</i>	< 1 } 38.2 }	< 1 } 33.3 }	33.3 } 48.8 }	4.3 } 4.3 }	< 1 } 5.1 }	5.1 } 4.9 }	7.2 } 7.2 }
313	—	2806	not obs.	7.0	7.5	14.9	—	0.9	—	—
621 } 522 }	2843 } 2848 }	2842 } 2848 }	<i>w</i>	14.1 } 74.3 }	10.1 } 79.3 }	89.4 } 98.7 }	11.9 } 11.9 }	1.8 } 9.5 }	12.2 } 12.5 }	14.4 } 14.4 }
541	—	2907	not obs.	15	10.4	14.8	not obs.	1.9	1.3	1.8
631 } 532 }	3166 } 3167 }	3161 } 3167 }	<i>m</i>	9.8 } 308 }	9.4 } 322 }	331 } 332 }	332 } 36.1 }	1.1 } 35.1 }	36.2 } 37.7 }	37.6 } 37.6 }

v = very; *w* = weak; *m* = medium; *s* = strong.

The powder photographs were a little spotty, making the visual estimation of lines more difficult than for ReMo55. The small differences in the results for the two alloys led to the two order schemes given in Table 5. For the purposes of ordering the unit cell was assumed to contain 20 Re atoms and 10 Mo atoms. The limited data given in Table 6, for low-angle lines only, do not warrant an unequivocal acceptance of either scheme but calculations on higher-angle lines favour scheme No. 1.

Discussion

The order schemes obtained by other workers for σ -phases are presented for comparison with the present results in Table 7. The σ -phase Re₁₈Mo₁₂ studied by Ageev & Shekhtman (1959) has a composition intermediate between those of the two Re-Mo alloys used in this work and the present results suggest the following ordering scheme for this alloy: *A*-2Re; *B*-1Re3Mo; *C*-4Re4Mo; *D*-7Re1Mo;

Table 7

Unit-cell size	Re ₁₈ Mo ₁₂ ⁽¹⁾	Re ₁₈ Cr ₁₂ ⁽²⁾	Re ₂ Cr ⁽³⁾	Mn ₃ Cr ⁽⁴⁾	Mn ₁₀ Mo ₁₁ ⁽⁵⁾	Re _{16.5} Mo _{13.5} ⁽⁶⁾	Re ₂₀ Mo ₁₀ ⁽⁶⁾
<i>a</i>	9.54 Å	—	9.290 Å	—	9.10 Å	9.601 Å	9.579 Å
<i>c</i>	4.95	—	4.831	—	4.74	4.985	4.974
<i>c/a</i>	0.52	—	0.52	—	0.52	0.519	0.519
Site							
<i>A</i>	Re	Re	Assumed	Mn	Mn	Re	Re
<i>B</i>	Mo	Cr	Disordered	3Mn, 1Cr	Mo	1Re, 3Mo	2Re, 2Mo
<i>C</i>	Re	Re		5Mn, 3Cr	5Mn, 3Mo	4Re, 4Mo	4Re, 4Mo
<i>D</i>	Re	Re		Mn	Mn	6.5Re, 1.5Mo	Re
<i>E</i>	Mo	Cr		4.5Mn, 3.5Cr	4Mn, 4Mo	3Re, 5Mo	4Re, 4Mo

(¹) Ageev & Shekhtman, 1959. (²) Ageev & Shekhtman, 1960. (³) Waterstrat & Kasper, 1957.
 (⁴) Kasper & Waterstrat, 1956. (⁵) Decker *et al.*, 1954. (⁶) Present results.

E -4Re4Mo. This shows agreement with Ageev & Shekhtman for A , B and D sites only, and furthermore, Ageev & Shekhtman reject an order scheme with C and E sites filled in the manner suggested. Unfortunately, no comparable details of line intensities are given in their paper.

It is interesting to compare the present order schemes for σ Re-Mo with those of σ Mn-Cr and σ Mn-Mo, since manganese and rhenium on the one hand and Mo and Cr on the other belong to the same group in the periodic table. The order schemes for σ Mn-Cr and σ Mn-Mo are almost alike with Cr and Mo playing the same role and the excess Mn atoms in Mn_3Cr tending to fill up B sites rather than C and E sites. The proposed schemes for ReMo55 and ReMo68 are very similar, with Re behaving like Mn and Mo behaving like Cr, except in the filling of B sites. It follows from this comparison that the chemical factor associated with the positions of the alloying elements in the periodic table is an important one in deciding the nature of the order in σ -phases. In contrast to this, it has been noted by Greenfield & Beck (1956) that the mean compositions of the σ -phases formed by rhenium correspond closely to that of σ Mn-Mo but not σ Mn-Cr.

Assuming Re behaves like Mn, σ Re-Cr should be ordered like σ Mn-Cr and σ Re-Mo, but the results given in Table 7 are conflicting on this point. Ageev & Shekhtman give the same order scheme for σ ReCr as σ ReMo, whilst Waterstrat & Kasper (1957) state that their σ ReCr is disordered. A more detailed analysis of this phase is required because the Ageev & Shekhtman scheme is based on six strong lines only and the Waterstrat & Kasper scheme is derived from a 5 cm powder film. As noted above, the main evidence for order is obtained from a detailed study of weak lines.

For σ -phases formed between metals of the first long period and also with molybdenum, a correlation between the position of the element to the left (X) or to the right (Y) of manganese in the periodic table, the co-ordination number and effective volume of site occupied in the ordered structure has been noted by Kasper & Waterstrat (1956) as follows:

Site	Co-ordination		Occupancy
	No.	Volume of site	
A	12	Small	Y
B	15	Large	X
C	14	Medium	Mixed
D	12	Small	Y
E	14	Medium	Mixed

This correlation is maintained approximately by the σ -phase discussed above formed by rhenium from the third long period and molybdenum from the

second long period, with rhenium behaving like Y . In σ ReFe the same correlation is observed with Re behaving like X (Ageev & Shekhtman, 1960) and this dual role is similar to that of manganese itself, which also behaves like X and Y (Kasper & Waterstrat, 1956).

Further correlations have been sought between alloying elements in σ -phases and observed order and, in particular, it has been noted that the volume associated with the crystallographic sites is in accordance with the size of the atomic radii of the elements. This is not applicable to Re and Mo which have very similar radii: $r_{Re}=1.37$ and $r_{Mo}=1.38$ Å, and the main conclusion which can be drawn from the present work is that rhenium acts like manganese in its ordering behaviour in σ -phases.

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